

3 Strikes Yer Out!


Group Members:

1. $\lim _{x \rightarrow-2} \frac{x^{2}+1}{3 x^{2}-2 x+5}$
2. $\lim _{x \rightarrow 0} \frac{\sin 2 x}{3 x}=\lim _{x \rightarrow 0} \frac{\frac{2}{3} \sin 2 x}{\frac{2}{3} \cdot 3 x}$

$$
=\frac{(-2)^{2}+1}{3(-2)^{2}-2(-2)+5}=\frac{5}{21}
$$

$=\frac{2}{3} \lim _{x \rightarrow 0} \frac{\sin 2 x}{2 x}=\frac{2}{3}$
3. $\lim _{x \rightarrow 0}\left(e^{x} \sin x\right)=e^{0} \cdot \sin 0$
4. $\lim _{x \rightarrow 1} \frac{x^{2}-1}{2 x^{2}-x-1}=\lim _{x \rightarrow 1} \frac{(x-1)(x+1)}{(2 x+1)(x-1)}$

$$
=1 \cdot 0=0
$$

$=\lim _{x \rightarrow 1} \frac{x+1}{2 x+1}=\frac{2}{3}$
5. $\lim _{x \rightarrow 0} \frac{\tan x}{x}=\lim _{x \rightarrow 0} \frac{\frac{\sin x}{\cos x}}{x}$
6. $\lim _{x \rightarrow 4} \sqrt{1-2 x}=\sqrt{1-2(y)}=\sqrt{-7}$

$$
\begin{aligned}
& =\lim _{x \rightarrow 0} \frac{\sin x}{x} \cdot \frac{1}{\cos x}=\lim _{x \rightarrow 0} \frac{\sin x}{x} \cdot \operatorname{lin}_{x \rightarrow 0} \frac{1}{\cos x} \\
& =1 \cdot 1=1
\end{aligned}
$$


$\qquad$

1. $\lim _{x \rightarrow-\infty} \frac{2 x^{2}+3}{5 x^{2}+7}=\lim _{x \rightarrow-\infty} \frac{2 x^{2}}{5 x^{2}}$
2. $\lim _{x \rightarrow \infty} \frac{x}{e^{x}}=\square$

$$
=\frac{2}{5}
$$

3. $\lim _{x \rightarrow \infty} \frac{x^{3}-4 x^{2}+3 x+3}{x-3}$
4. $\lim _{x \rightarrow-\infty} \frac{5-x^{4}}{x^{3}+2}=\lim _{x \rightarrow-\infty} \frac{-x^{4}}{x^{3}}$

$$
=\lim _{x \rightarrow \infty} \frac{x^{3}}{x}=\lim _{x \rightarrow \infty} x^{2}=\infty
$$

$=\lim _{x \rightarrow-\infty}-x=\infty$
5. Find the vertical asymptote (s) and use limits to describe the behavior to the left and right of the asymptote (s).

$$
f(x)=\frac{x+3}{2-x}
$$

V.A. $: x=2$

$$
\begin{aligned}
& \lim _{x \rightarrow 2^{+}} f(x)=-\infty \\
& \lim _{x \rightarrow 2^{-}} f(x)=\infty
\end{aligned}
$$

6. Find a right and left end behavior model for the function.

$$
f(x)=-3 x+e^{x}
$$

R.E.B.m.: $e^{x}$
L. E.B.m: $-3 x$


1. What are the 4 different types of discontinuity?

Infinite, removable, jump, oscillating.
2. Find all discontinuities of the function and give what type each is:

$$
f(x)=\frac{5 x^{2}-13 x-6}{3 x^{2}-5 x-12}=\frac{(5 x+2)(x-3)}{(3 x+4)(x-3)}
$$

Infinite disc. $: x=\frac{-4}{3}$
Remove disc.: $x=3$
3. Is the function continuous or not? Explain why or why not.

$$
f(x)= \begin{cases}x^{2}+5, x \geq 1 & \lim _{x \rightarrow 1^{+}} f(x)=6 \\ 12 x-5, x<1 & \lim _{x \rightarrow 1^{-}} f(x)=7\end{cases}
$$

Not continues, since $\lim _{x \rightarrow 1} f(x)$ $\partial N \varepsilon$.
4. Find the value (s) of " $c$ " such that $\mathrm{f}(\mathrm{x})$ is continuous at $\mathrm{x}=2$.

$$
f(x)=\left\{\begin{array}{l}
c^{2} x+5, x \geq 2 \\
x+8, x<2
\end{array}\right.
$$

$$
c \cdot 2+s=
$$

$$
2 c^{2}+5=10
$$

$$
2 c^{2}=5
$$



$$
c= \pm \sqrt{\frac{5}{2}}
$$

1. Find the average rate of change of $f(x)=x^{3}+2$ over [2,5]. $3 \frac{39}{\frac{117}{27}}$

$$
\begin{aligned}
\text { avg. rate of change } & =\frac{f(5)-f(2)}{5-2}=\frac{127-10}{3}=\frac{117}{3} \\
& =39
\end{aligned}
$$

2. Find the slope of the curve $f(x)=\frac{1}{1-x}$ at $\mathrm{x}=4$.

$$
\begin{aligned}
& \lim _{h \rightarrow 0} \frac{f(4+h)-f(x)}{h}=\lim _{h \rightarrow 0} \frac{\frac{-3-h}{}+\frac{1}{13}}{h}=\lim _{h \rightarrow 0} \frac{\frac{3+-3-h}{3(-3-h)}}{h} \\
= & \lim _{h \rightarrow 0} \frac{\frac{-h}{3(-3-h)}}{h}=\lim _{h \rightarrow 0} \frac{-1}{3(-3-h)}=\frac{-1}{-9}=\frac{1}{9}
\end{aligned}
$$

3. Find the equation of the normal line of $f(x)=x^{2}+3 x+5$ at $\mathrm{x}=-2$.

$$
\begin{aligned}
& \lim _{h \rightarrow 0} \frac{f(-2+h)-f(-2)}{h}=\lim _{h \rightarrow 0} \frac{(-2+h)^{2}+3(-2+h)+5-3}{h} \\
= & \lim _{h \rightarrow 0} \frac{4\left(-4 h+h^{2}-h+3 h+5-5\right.}{h}=\lim _{h \rightarrow 0} \frac{h^{2}-h}{h}
\end{aligned}
$$

$$
=\lim _{h \rightarrow 0} \frac{h(h-1)}{h}=-1 \quad \begin{aligned}
& m=1 \in \text { normal } \\
& \text { Names: }
\end{aligned}
$$

$\qquad$
$\qquad$
$\qquad$

| Worksheet | 1st <br> Attempt - <br> 3 points | $2^{\text {nd }}$ Attempt - <br> 2 points | $3^{\text {rd }}$ Attempt - <br> HIGH FIVE! |
| :---: | :---: | :---: | :---: |
| A |  |  |  |
| B |  |  |  |
| C |  |  |  |
| D |  |  |  |
| Total Points |  |  |  |

## 3 Strikes Yer Out Rules

1) Each worksheet has 3-6 problems. After you are done, bring up the one you finished for grading.
2) You must work together so that each group member is at the same pace.
**Note: Hitchhiking is illegal in Calculus!!**
3) When your whole group is finished with the worksheet, one person should bring ALL worksheets to check with me. Bring your score sheet with you!!
4) Scoring:

- If your group gets $A L L$ problems correct the first time, you will receive 3 points (to be written on the score sheet).
- Otherwise, you will have to take your sheet, go back, and correct them....on the second time, you will receive 2 points.
- ....on the third time...it's a HIGH FIVE FOR YOU!!


## Good Luck!!

