

1. Let f be twice differentiable for all real numbers.

a. What does this information tell you about f ? Circle the answer(s) that apply.

f exists f is differentiable f is continuous

b. What does this information tell you about f' ? Circle the answer(s) that apply.

f' exists f' is differentiable f' is continuous

c. What does this information tell you about f'' ? Circle the answer(s) that apply.

f'' exists f'' is differentiable f'' is continuous

d. Let $f(2) = 0$ and $f(6) = 12$. What theorem allows you to conclude that there exists a c in the interval $(2, 6)$ such that $f(c) = 8$?

The Intermediate Value Theorem

e. Let $f(2) = 0$ and $f(6) = 12$. What theorem allows you to conclude that there exists a c in the interval $(2, 6)$ such that $f'(c) = 3$?

The Mean Value Theorem

2. Let $B(t)$ be a differentiable function given at select values in the table.

t	0	3	5	15
$B(t)$	-2	4	0	6

a. Estimate $B'(4)$.

$$\frac{0 - 4}{5 - 3} = \frac{-4}{2} = -2$$

b. What can you say about $B(10)$?

- I. $B(10) > 0$
- II. $B'(10) > 0$
- III. $B''(10) > 0$

I only

II only

III only

I, II, and III

None of the choices

3. If $f(3) = 5$ and $f'(3) = 4$ and $g(x) = f^{-1}(x)$, then

A. $g'(3) = \frac{1}{4}$

B. $g'(5) = \frac{1}{4}$

C. $g'(4) = \frac{1}{5}$

D. $g'(5) = \frac{1}{3}$

Remember, horizontal shifts produce equivalent integrals!

4. Write the following limits as integrals.

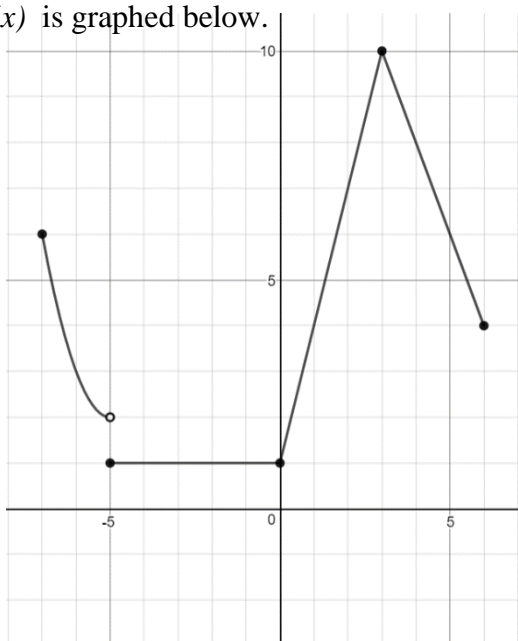
a. $\lim_{n \rightarrow \infty} \frac{1}{n} \left[\sqrt{\frac{1}{n}} + \sqrt{\frac{2}{n}} + \dots + \sqrt{\frac{n}{n}} \right] = \int_0^1 \sqrt{x} \, dx$

b. $\lim_{n \rightarrow \infty} \left(\frac{1}{n} \left(\left(9 + \frac{1}{n}\right)^2 + \left(9 + \frac{2}{n}\right)^2 + \left(9 + \frac{3}{n}\right)^2 + \left(9 + \frac{4}{n}\right)^2 + \dots + \left(9 + \frac{n}{n}\right)^2 \right) \right) = \int_0^1 (9+x)^2 \, dx$
 OR $\int_9^{10} x^2 \, dx$

c. $\lim_{n \rightarrow \infty} \left(\frac{3}{n} \left(\ln(2) + \ln\left(2 + \frac{3}{n}\right) + \ln\left(2 + \frac{6}{n}\right) + \dots + \ln\left(2 + \frac{3(n-1)}{n}\right) \right) \right) = \int_0^3 \ln(2+x) \, dx$
 OR $\int_2^5 \ln x \, dx$

d. $\lim_{n \rightarrow \infty} \left(\frac{7}{n} \left(\sqrt[3]{-2 + \frac{7}{n}} + \sqrt[3]{-2 + \frac{14}{n}} + \sqrt[3]{-2 + \frac{21}{n}} + \sqrt[3]{-2 + \frac{28}{n}} + \dots + \sqrt[3]{-2 + \frac{7n}{n}} \right) \right) = \int_0^7 (-2+x)^{1/3} \, dx$
 OR $\int_{-2}^5 x^{1/3} \, dx$

5. $f(x)$ is graphed below.



$f(x)$ is ... (circle all that apply)

- I. continuous everywhere in the interval $[-7, 6]$.
- II. differentiable everywhere in the interval $[-7, 6]$.
- III. continuous, but not differentiable at $x = 0$.
- IV. continuous and differentiable at $x = 2$.
- V. not continuous and not differentiable at $x = -5$.