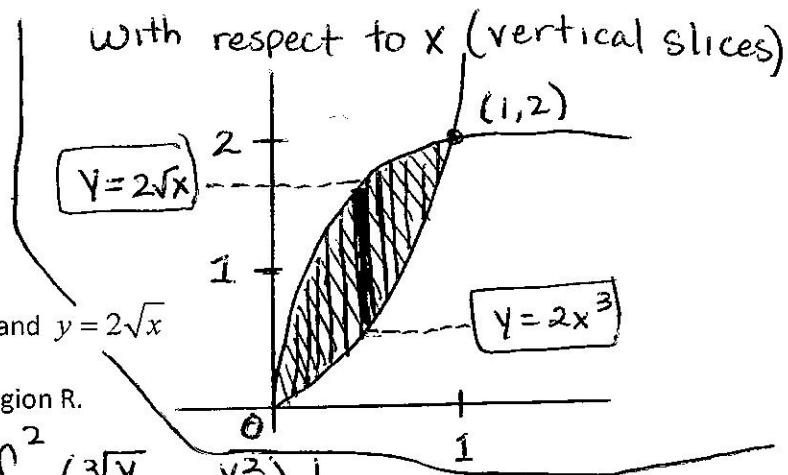


# KEY

## AP Calculus AB 7.3 Area/Volume Review


Let R be the region enclosed by the curves  $y = 2x^3$  and  $y = 2\sqrt{x}$




1. Write an integral representing the area of region R.

vertical slices  $\rightarrow \int_0^1 (2\sqrt{x} - 2x^3) dx$     or     $\int_0^2 \left( \sqrt{\frac{y}{2}} - \frac{y^2}{4} \right) dy$   $\leftarrow$  Horizontal slices

2. Write an integral representing the volume of a solid formed such that cross sections taken perpendicular to the x-axis are squares with one side running between the two curves.

vertical slices  $\int_0^1 (2\sqrt{x} - 2x^3)^2 dx$      $\left( \text{Area} = (\text{side})^2 \right)$   


3. Write an integral representing the volume of a solid formed such that cross sections taken perpendicular to the y-axis are isosceles right triangles with one leg running between the two curves.

Horizontal slices  $\int_0^2 \frac{1}{2} \left( \sqrt{\frac{y}{2}} - \frac{y^2}{4} \right)^2 dy$      $\left( \text{Area} = \frac{1}{2} (\text{side})^2 \right)$   


4. Write an integral representing the volume of the solid formed by revolving R about the...

a) x-axis  $\int_0^1 \left( \pi (2\sqrt{x} - 0)^2 - \pi (2x^3 - 0)^2 \right) dx$

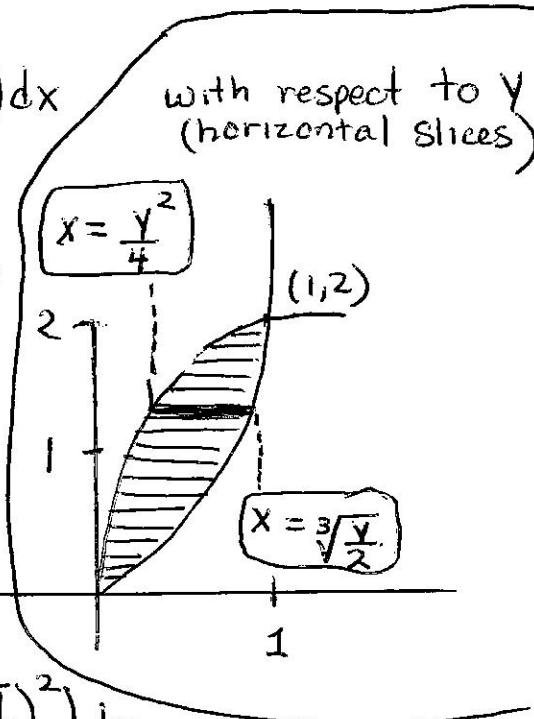
b) y-axis  $\int_0^2 \left( \pi \left( \sqrt{\frac{y}{2}} - 0 \right)^2 - \pi \left( \frac{y^2}{4} - 0 \right)^2 \right) dy$

c) Line  $x = -3$   $\int_0^2 \left( \pi \left( \sqrt{\frac{y}{2}} - (-3) \right)^2 - \pi \left( \frac{y^2}{4} - (-3) \right)^2 \right) dy$

d) Line  $y = 2$   $\int_0^1 \left( \pi (2 - 2x^3)^2 - \pi (2 - 2\sqrt{x})^2 \right) dx$

\* e) Line  $x = 5$   $\int_0^2 \left( \pi \left( 5 - \frac{y^2}{4} \right)^2 - \pi \left( 5 - \sqrt{\frac{y}{2}} \right)^2 \right) dy$

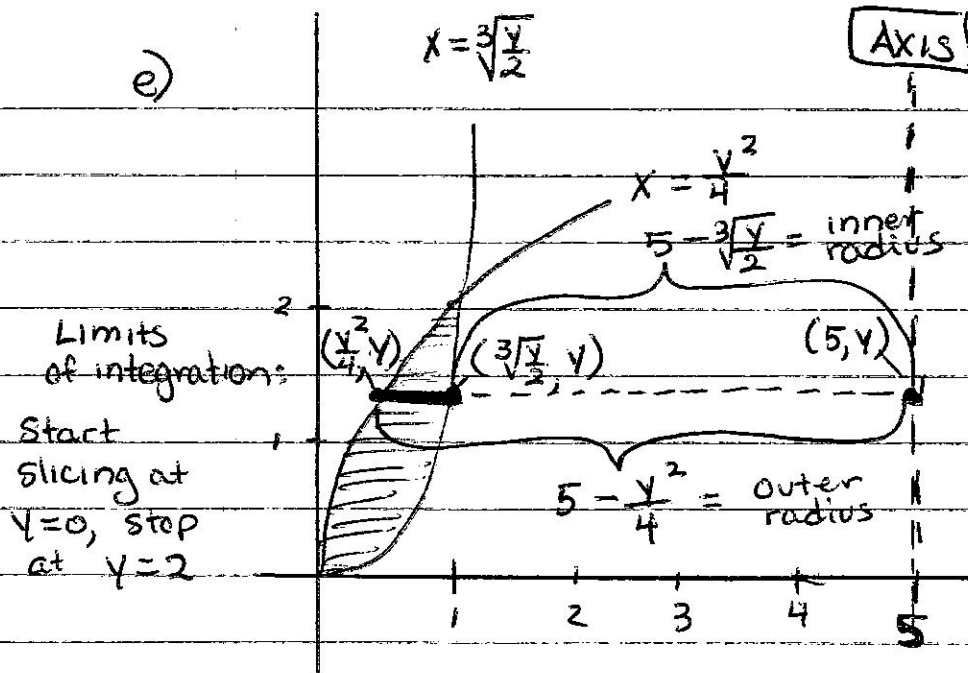
\* f) Line  $y = -1$   $\int_0^1 \left( \pi (2\sqrt{x} - (-1))^2 - \pi (2x^3 - (-1))^2 \right) dx$



always slice perpendicular to axis of revolution

\* see diagrams

e)

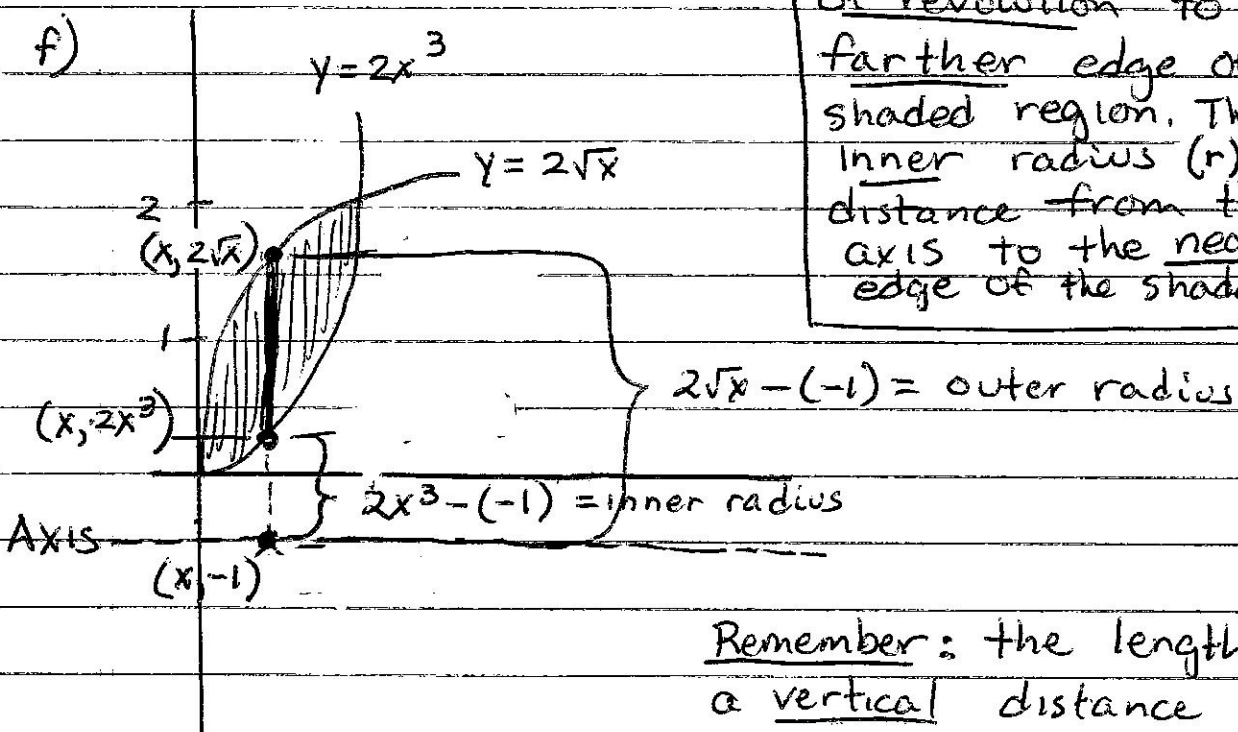


REMEMBER: THE length of a horizontal distance is always measured "RIGHT MINUS LEFT"

WASHERS  $\pi R^2 - \pi r^2$

The Outer radius ( $R$ ) is always the distance from the axis of revolution to the farther edge of the shaded region. The Inner radius ( $r$ ) is the distance from the axis to the nearer edge of the shaded region.

f)



Remember: the length of a vertical distance is always measured "top minus bottom"

Limits of integration: Start slicing at  $x=0$ , stop at  $x=1$