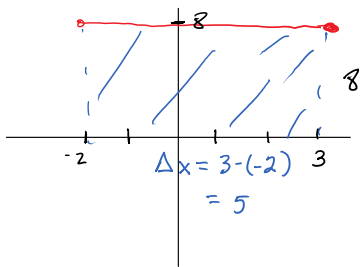


Graph $f(x)=8$ over the interval $[-2, 3]$



Area under the curve
to the x-axis?

$$5(8) = 40$$

★ Area under a curve
 $= \int_a^b f(x) dx$ iff $f(x)$

in non-negative

$$\int_{-2}^3 f(x) dx = \int_{-2}^3 8 dx = 8(3 - (-2)) = 8(5) = 40$$

Theorem: The integral of a constant

If $f(x) = c$ where $c = \text{constant}$
on the interval $[a, b]$, then

$$\int_a^b f(x) dx = \int_a^b c dx = c(b-a)$$

you try.. Evaluate $\int_{-2}^3 -8 dx = -8(3 - (-2)) = -40$

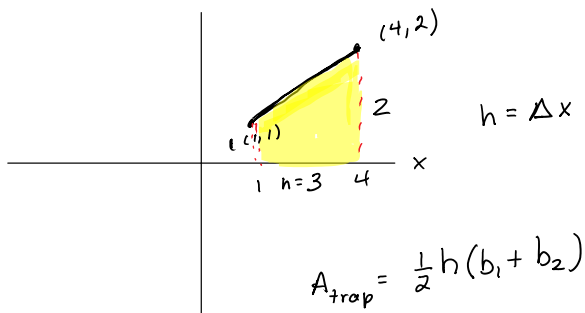


Evaluating Integrals using Geometry.

Evaluate!

$f(x)$

$$\begin{aligned}
 a. \int_1^4 \left(\frac{1}{3}x + \frac{2}{3}\right) dx &= \\
 &= \frac{1}{2}(3)(2+1) = \frac{1}{2}(3)(3) \\
 &= 9/2
 \end{aligned}$$

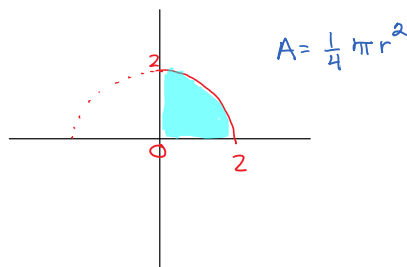


recall: $x^2 + y^2 = r^2$

$$\begin{aligned}
 y &= \sqrt{r^2 - x^2} \\
 y &= -\sqrt{r^2 - x^2}
 \end{aligned}$$

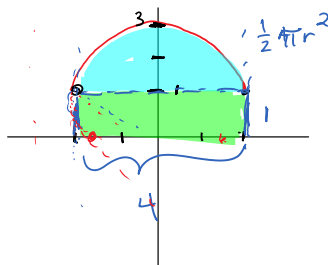
evaluate: $\int_0^2 \sqrt{4-x^2} dx$

$$\begin{aligned}
 &= \frac{1}{4}\pi(2)^2 \\
 &= \pi
 \end{aligned}$$



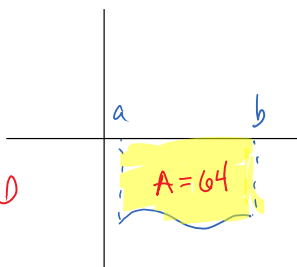
you try... $\int_{-2}^2 (1 + \sqrt{4-x^2}) dx$

$$\begin{aligned}
 &= \frac{1}{2}\pi(2)^2 + 4(1) \\
 &= 2\pi + 4
 \end{aligned}$$



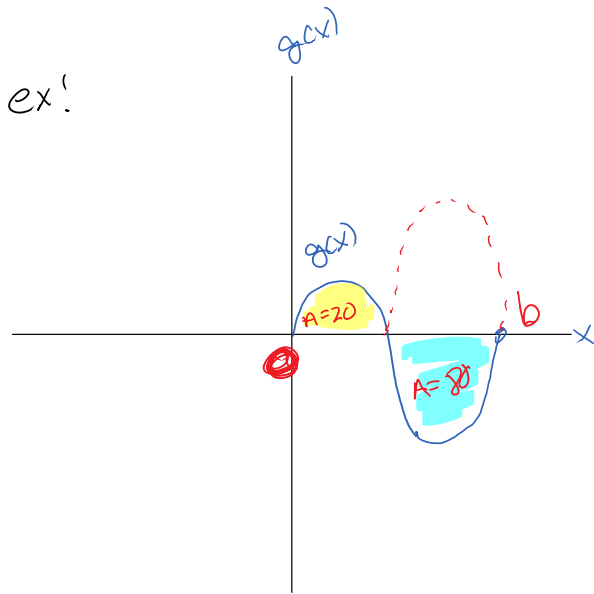
$f(x) < 0$? $\int_a^b f(x) dx$

$= -64$
value of integral



Net Area: refers to the "positive" area combined w/ the "negative" area

Integral value $\int_a^b f(x) dx = \text{Area above (x-axis)} - \text{area below (x-axis)}$



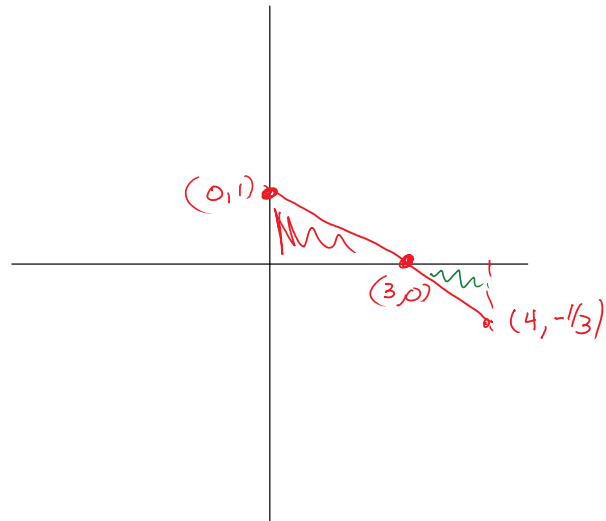
$$\int_0^b g(x) dx = 20 - 80 = -60$$

$$\text{Area} = \int_0^b |g(x)| dx = 20 + 80 = 100$$

ex. evaluate $\int_0^4 (-\frac{1}{3}x + 1) dx$

$$= \frac{1}{2}(3)(1) - \frac{1}{2}(1)(\frac{1}{3})$$

$$= \frac{3}{2} - \frac{1}{6} = \frac{8}{6} = \frac{4}{3}$$



★ use calculator to check above problem

you try $\int_0^{\pi} x \sin x dx$

you try

$$\int_0^{\pi} x \sin x dx$$