## Intermediate Value Theorem...Extreme Value Theorem...Mean Value Theorem...Oh, My!

## Intermediate Value Theorem (IVT)

A function $y=f(x)$ that is continuous on a closed interval $[a, b]$ takes on every value between $f(a)$ and $f(b)$.
In other words, if $y_{0}$ is between $f(a)$ and $f(b)$, then $y_{0}=f(c)$ for some $c$ in $[a, b]$.


## The Extreme Value Theorem (EVT)

If $f$ is continuous on a closed interval $[a, b]$,
then $f$ has both a maximum value and a minimum value on the interval.

## The Mean Value Theorem (MVT) for Derivatives

If $y=f(x)$ is continuous at every point of the closed interval $[a, b]$ and differentiable at every point of its $(a, b)$, then there is at least one point $c$ in $(a, b)$ at which


$$
f^{\prime}(c)=\frac{f(b)-f(a)}{b-a}
$$

