

#1-11 cover 1.1 and 1.2 #12-16 cover 1.3

- 1) Be able to use your calculator to create scatterplots, lists and recognize grapher failure.
- 2) Be able to solve application problems with volume, distance and free fall.
- 3) Be able to solve radical equations.
- 4) Be able to determine if a relation is a function from the equation.
- 5) Be able to find the domain of a function from the equation.
- 6) Be able to determine the range of a function from a graph.
- 7) Be able to determine
- 8) Be able to find max/min and increasing and decreasing intervals.
- 9) Be able to determine if a function is even or odd.
- 10) Be able to find the horizontal, vertical and end behavior asymptotes.
- 11) Be able to evaluate limits.
- 12) Be able to graph the 12 basic functions.
- 13) Be able to graph with transformations.
- 14) Be able to graph real world situations.
- 15) Be able to graph functions with more than one horizontal asymptote.
- 16) Be able to graph a piecewise determined function.

1. **U.S. Petroleum Exports** The average U.S. exports of petroleum for the years 2001–2011, in thousands of barrels per day, are shown in Table 1.15.



**Table 1.15 Daily U.S. Oil Exports**

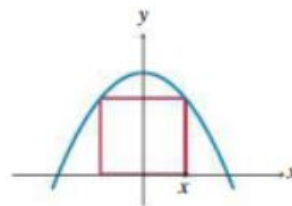
Year	Exports (1000 bbl./day)
2001	971
2002	984
2003	1027
2004	1048
2005	1165
2006	1317
2007	1433
2008	1802
2009	2024
2010	2353
2011	2924

Source: *Monthly Energy Review*, Aug. 2012, as reported in *The World Almanac and Book of Facts 2013*.

- (a) Sketch a scatter plot of export numbers ( $y$ ) as a function of years since 2000 ( $x$ ).
- (b) Use quadratic regression to model the data with a quadratic function and superimpose the parabolic curve on the scatter plot. Is it a good fit?
- (c) Based on the quadratic model, approximately how many thousands of barrels of oil would the United States export per day in 2016?

2. **Inscribing a Rectangle Under a Parabola**

A rectangle is inscribed between the  $x$ -axis and the parabola  $y = 36 - x^2$  with one side along the  $x$ -axis, as shown in the figure below.



- (a) Let  $x$  denote the  $x$ -coordinate of the point denoted in the figure. Write the area  $A$  of the rectangle as a function of  $x$ .
- (b) What values of  $x$  are in the domain of  $A$ ?
- (c) Sketch a graph of  $A(x)$  over the domain.
- (d) Use your grapher to find the maximum area that such a rectangle can have.

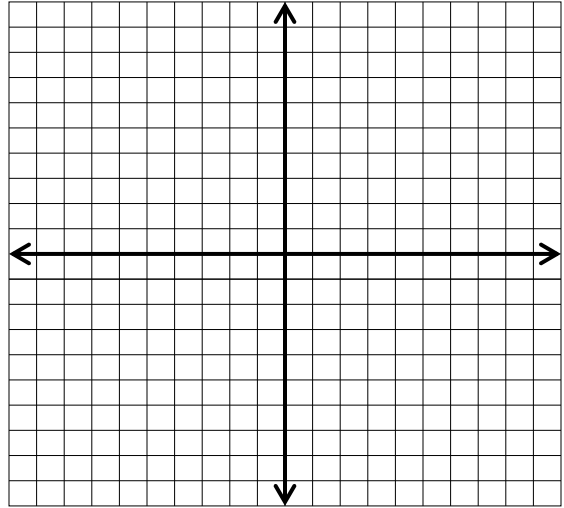
3. Solve algebraically  $x = -1 + 2\sqrt{x+4}$

4. Function?  $y - x = x^2 - |y|$

5. Sketch a complete graph of the function and then determine whether the function is continuous or discontinuous

a.  $f(x) = \begin{cases} x^2 + 5 & x \geq 0 \\ -|x+3| & x < 0 \end{cases}$

b. Continuous or discontinuous?



c.  $\lim_{x \rightarrow 0^-} f(x) = \underline{\hspace{2cm}}$        $\lim_{x \rightarrow 0^+} f(x) = \underline{\hspace{2cm}}$

d.  $f(0) = \underline{\hspace{2cm}}$

6. Given  $f(x) = \frac{6x^2 - x - 1}{2x^2 + 9x - 5}$  State:

Domain (without a calculator):

Range (using a calculator):

State all types of discontinuities:

Is there a Horizontal Asymptote?

End behavior:  $\lim_{x \rightarrow \infty} g(x) = \underline{\hspace{2cm}}$

$\lim_{x \rightarrow -\infty} g(x) = \underline{\hspace{2cm}}$

Other limits:  $\lim_{x \rightarrow -5^-} g(x) = \underline{\hspace{2cm}}$

$\lim_{x \rightarrow -5^+} g(x) = \underline{\hspace{2cm}}$

$\lim_{x \rightarrow \frac{1}{2}^-} g(x) = \underline{\hspace{2cm}}$

$\lim_{x \rightarrow \frac{1}{2}^+} g(x) = \underline{\hspace{2cm}}$

7. Look at the graph from #6 on your graphing calculator and determine the following:

Increasing intervals \_\_\_\_\_ Decreasing Intervals \_\_\_\_\_ Constant Intervals \_\_\_\_\_

8. On which intervals is the function  $g(x) = x^4 - 1.1x^2 - 65.4x + 229.5$  increasing? Give your answer using 3 decimal places. (Calculator OK)

9. Perform the tests to determine whether the function  $h(x) = x^4y^2 - 3xy$  is odd, even or neither.

10. Graph a function that meets all of the following:

a.  $\lim_{x \rightarrow \infty} f(x) = 3$

$\lim_{x \rightarrow -\infty} f(x) = 3$

$f(0) = -2$

decreases on  $(-\infty, 2]$

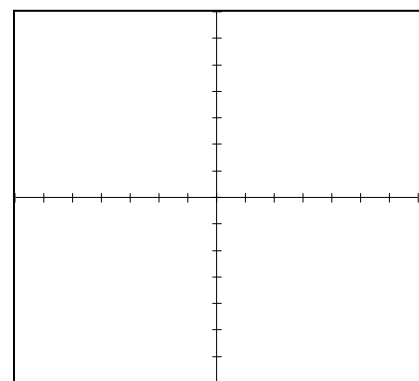
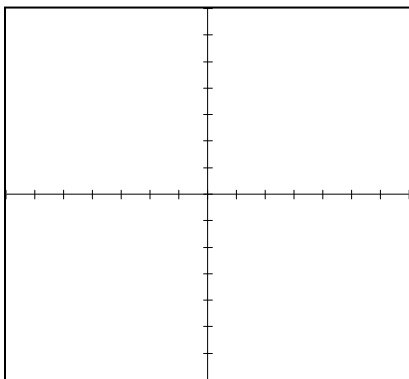
increases on  $[2, \infty)$

b.  $\lim_{x \rightarrow \infty} f(x) = \infty$

$\lim_{x \rightarrow -\infty} f(x) = -\infty$

$f(-4) = 0$

increases on its entire domain



11-12 Given:  $f(x) = x$ ,  $f(x) = x^2$ ,  $f(x) = x^3$ ,  $f(x) = \frac{1}{x}$ ,  $f(x) = \sqrt{x}$ ,  $f(x) = \frac{1}{1+e^{-x}}$   
 $f(x) = e^x$ ,  $f(x) = \ln x$ ,  $f(x) = \sin x$ ,  $f(x) = \cos x$ ,  $f(x) = |x|$ ,  $f(x) = \text{int}(x)$

11. Which six functions that are increasing on their entire domains?

12. Which three functions have end behavior  $\lim_{x \rightarrow -\infty} f(x) = 0$ .

13. Use your graphing calculator to determine all local and absolute extrema and where they occur. Also state if the function is bounded above, bounded below, bounded, or unbounded.

a.  $y = x^3 - 3x$

b.  $y = \frac{4x^2}{x^2 + 4}$

c.  $y = (x+1)^2 - 7$